Table 4. Hydrogen-bond distances ( $\AA$ ) and angles ( ${ }^{\circ}$ )

packing is influenced by hydrogen bonding. In both molecules all available H atoms participate in intermolecular hydrogen bonds (parameters are given in Table 4). In (I) water crystallized with the quinoline. The $\mathrm{H}_{2} \mathrm{O}$ acts as a donor in hydrogen bonds to two different $\mathrm{O}(13)$ atoms and as an acceptor from one of the H atoms on $\mathrm{N}(1)$. The remaining H on $\mathrm{N}(1)$ acts as a donor to $\mathrm{O}(12)$. In addition to the hydrogen bonds there is one intermolecular approach less than van der Waals distances, $\mathrm{C}(2) \cdots \mathrm{C}(2)$ at $3.42 \AA$. In (II) there is only one H available for hydrogen bonding and it acts
as a donor to O (13). There are no other approaches in (II) which are less than van der Waals separations.

## References

Busing, W. R., Martin, K. O., Levy, h. A., Ellison, R. D., Hamilton, W. C., Ibers, J. A., Johnson, C. K. \& Thiessen, W. E. (1975). ORXFLS. Oak Ridge National Laboratory, Tennessee.
Flippen-Anderson, J. L., Gllardi, R. \& Konnert, J. H. (1983). RESLSQ. NRL Report 5042. Naval Research Laboratory, Washington, DC.
Gilardi, R. D (1973). Acta Cryst. B29, 2089-2095.
Johnson, C. K. (1965). ORTEPII. Report ORNL-3794, revised. Oak Ridge National Laboratory, Tennessee.
Karle, J. \& Karle, I. L. (1966). Acta Cryst. 21, 849-859.
Main, P., Fiske, S. J., Hull, S. E., Lessinger, L., Germain, G., Declerce, J.-P. \& Woolfson, M. M. (1980). MULTAN80. A System of Computer Programs for the Automatic Solution of Crystal Structures from X-ray Diffraction Data. Univs. of York, England, and Louvain, Belgium.
Schimitschek, E. J., Trias, J. A., Hammond, P. R., Henry, R. A. \& Atkins, R. L. (1976). Opt. Commun. 16, 313-316.

# A Structure Containing Diastereomers, (2S,4R)-trans- and (2R,4R)-cis-2-Hydroxy-2,4-dimethyl-3,4-dihydro-2H,5H-pyrano[3,2-c][1]benzopyran-5-one, $\mathrm{C}_{14} \mathrm{H}_{14} \mathrm{O}_{4}$ 

By Edward J. Valente* and Verner Schomaker<br>Department of Chemistry, University of Washington, Seattle, Washington 98195, USA

(Received 14 October 1983; accepted 10 February 1984)

Abstract. $M_{r}=246 \cdot 3$, monoclinic, $P 2_{1}, a=7.804$ (3), $b=18.248$ (8), $\quad c=8.752$ (5) $\AA, \quad \beta=99.59^{\circ}, \quad V=$ $1233 \AA^{3}, Z=4$ ( 2 molecules/asymmetric unit), $D_{x}$ $=1.33 \mathrm{~g} \mathrm{~cm}^{-3}, \quad \lambda(\mathrm{Mo} K \alpha)=0.71067 \AA, \quad \mu=$ $0.91 \mathrm{~cm}^{-1}, F(000)=520, T=293 \mathrm{~K}$. Final $R=0.066$ for 1123 observed independent intensities. The structure consists of diastereomers approximately inversionrelated through a pseudocenter of symmetry at $x$ $=0.241$ (4), $z=0.281$ (3) except the 4 -methyl groups. The dihydropyran rings are half chairs distorted towards the $e, f$-diplanar conformation. Like molecules are hydrogen-bonded between hydroxyl and carbonyl groups along a, $\mathrm{O} \cdots \mathrm{O}$ distances being 2.781 (7) (trans) and 2.780 (7) $\AA$ (cis).

Introduction. Michael-type addition of certain $\alpha, \beta$ unsaturated ketones with 4-hydroxycoumarin leads to

[^0]3-substituted 4-hydroxycoumarins. In solution these products exist in a dynamic equilibrium between diastereomeric hemiketals and the open (keto) form of the molecule. The compound so obtained using 3-penten-2-one ( $R=\mathrm{CH}_{3}$ ) consists of about equal parts of each isomer in chloroform solution (Valente, Santarsiero \& Schomaker, 1979), and its crystalline racemate consists of cis diastereomeric forms. As part of a structural study of this Michael addition product, we resolved the optical isomers and undertook a crystallographic investigation. In crystallizing the compound under different conditions, we hoped to observe another of the isomeric forms apparently present in solution.

© 1984 International Union of Crystallography

Table 1. Positional parameters $\left(\times 10^{4}\right)$ and $U_{e q}$ 's for cisand trans-2-hydroxy-2,4-dimethyl-3,4-dihydro-2H,5H-pyrano[3,2-c][1]benzopyran-5-one
E.s.d.'s are in parentheses.

|  | $\boldsymbol{x}$ | $y$ | $z$ | $U_{\text {eq }}\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| cis Isomer |  |  |  |  |
| $\mathrm{O}(1 /$ ) | -5465 (6) | 3950 (3) | -661 (6) | 7.2 (4) |
| O(2A) | -6192 (6) | 5016 (3) | 165 (7) | 9.4 (5) |
| $\mathrm{O}(3 A)$ | 635 (6) | 5317 (3) | 1072 (6) | 6.3 (4) |
| $\mathrm{O}(4 \mathrm{~A})$ | -385 (6) | 4172 (3) | 1560 (6) | 5.3 (4) |
| C(2A) | -5011 (11) | 4584 (5) | 166 (10) | 6.0 (7) |
| C(3A) | -3293 (12) | 4670 (3) | 962 (11) | 5.4 (7) |
| C(4A) | -2103 (11) | 4156 (5) | 835 (9) | 4.9 (6) |
| C(5A) | -1370 (12) | 2930 (5) | -226 (11) | 6.3 (7) |
| C(6A) | -1863 (14) | 2303 (6) | -1072 (12) | 7.8 (8) |
| $\mathrm{C}(7 A)$ | -3620 (18) | 2275 (6) | -1772 (11) | 8.6 (9) |
| $\mathrm{C}(8 A)$ | -4854 (13) | 2826 (7) | -1647 (12) | 7.9 (9) |
| C(9A) | -4247 (13) | 3410 (6) | -756 (11) | 5.3 (8) |
| C (10A) | -2535 (13) | 3482 (6) | -57 (11) | 5.0 (8) |
| C(11A) | -2812 (12) | 5336 (6) | 1892 (11) | 7.0 (8) |
| C (12A) | -1100 (9) | 5222 (4) | 3012 (9) | 5.4 (6) |
| C(13A) | 275 (11) | 4865 (4) | 2281 (9) | 5.5 (6) |
| C(14A) | 1872 (10) | 4641 (4) | 3360 (10) | 6.8 (7) |
| C(15A) | -2813 (9) | 6058 (4) | 932 (8) | $5 \cdot 3$ (7) |
| trans Isomer |  |  |  |  |
| O(1B) | 10285 (6) | 3199 | 6251 (5) | 5.8 (4) |
| $\mathrm{O}(2 \mathrm{~B})$ | 10992 (6) | 2090 (3) | 5570 (6) | 7.3 (4) |
| $\mathrm{O}(3 \mathrm{~B})$ | 4156 (6) | 1852 (3) | 4590 (6) | $6 \cdot 6$ (4) |
| $\mathrm{O}(4 B)$ | 5258 (5) | 2989 (3) | 4077 (5) | 5.2 (4) |
| $\mathrm{C}(2 B)$ | 9856 (11) | 2562 (5) | 5489 (9) | 5.9 (6) |
| C(3B) | 8080 (10) | 2462 (5) | 4662 (9) | 4.9 (6) |
| C(4B) | 6941 (8) | 3018 (4) | 4726 (8) | 4.0 (5) |
| $\mathrm{C}(5 B)$ | 6260 (9) | 4246 (5) | 5748 (9) | 5.9 (6) |
| $\mathrm{C}\left(6 B^{\prime}\right.$ | 6844 (13) | 4837 (5) | 6633 (11) | 6.8 (7) |
| $\mathrm{C}(7 B)$ | 8533 (13) | 4911 (5) | 7345 (10) | 6.2 (7) |
| $\mathrm{C}(8 B)$ | 9641 (13) | 4354 (5) | 7190 (9) | 5.7 (6) |
| C(9B) | 9059 (13) | 3732 (5) | 6326 (10) | 5.7 (7) |
| $\mathrm{C}(10 \mathrm{~B})$ | 7370 (12) | 3668 (5) | 5588 (9) | 4.3 (6) |
| $\mathrm{C}(11 B)$ | 7541 (11) | 1748 (5) | 3810 (10) | 5.4 (7) |
| $\mathrm{C}(12 \mathrm{~B})$ | 5887 (11) | 1902 (4) | 2646 (10) | 6.2 (7) |
| C(13B) | 4554 (10) | 2302 (5) | 3429 (9) | 5.5 (6) |
| C(14B) | 2952 (11) | 2540 (5) | 2327 (10) | 7.3 (7) |
| C(15B) | 8831 (13) | 1426 (6) | 2952 (12) | 10.2 (9) |

Experimental. Synthesis reported (Ikawa, Stahmann \& Link, 1944), resolved with brucine as more soluble salt and forms colorless crystals from ethanol:water. Crystal: $0.22 \times 0.27 \times 0.60 \mathrm{~mm}$, mounted along long axis, c. $D_{m}$ not measured. Weissenbergs: monoclinic with $0 k 0$ absent for $k$ odd. Picker FACS-1 diffractometer. Unit cell: least squares on 15 reflections ' $\pm 2 \theta$ '. Intensity measurements by $\omega$-scans, $1.0^{\circ} \mathrm{min}^{-1}$ in $\omega$, 30s backgrounds at scan limits, width $4 \cdot 1^{\circ}$, Mo $K \alpha$ radiation with 0.76 mm Nb filter; 3200 reflections $(h \pm 8, k 0 \rightarrow 23, \quad l 0 \rightarrow 10)$, to $\sin \theta / \lambda=0.65 \AA^{-1}$, in survey mode to pass by weak or absent reflections, 1247 measured exceeding their standard deviations, none requiring coincidence-loss correction. Four standards, for count and orientation, every 400 reflections, $1 \%$ decay over experiment. Structure discovered with MULTAN (Germain, Main \& Woolfson, 1971), two molecules in the asymmetric unit. Refinement: C and O positions and $U_{\text {iso }}$ 's by full-matrix least squares on all reflections except those with weighted $\left[\sigma^{2}(F)^{-1}\right]$ differences, $F_{o}-F_{\mathcal{c}}$ exceeding six. $U_{i j}$ for C and O included, then H's at calculated and fixed positions and their $U_{\mathrm{iso}}$ 's included; to $R=0.073$. Molecules refined individually in alternation to overcome model
divergence owing to pseudocentrosymmetrical structure. Final cycles of least squares in blocks on $F$, final $R=0.066, w R=0.031, S=1.67$ for 326 variables, scale factor 0.78 , with $f$ 's for C and O from International Tables for X-ray Crystallography (1974) and for H from Stewart, Davidson \& Simpson (1965); $(\Delta / \sigma)_{\mathrm{ave}}=0.06, \quad(\Delta / \sigma)_{\max }=0.25 \quad\{y[\mathrm{O}(4 A)]\}$, subsequent $\Delta \rho$ excursions $<0.4 \mathrm{e} \AA^{-3}$.

No corrections for anomalous dispersion, extinction or absorption. Crystals dissolved in acetonitrile give circular dichroism spectra with positive Cotton effects of increasing strength at 315,220 , and 210 nm , and a lone negative feature at 270 nm ; the same solution gives $a+$ optical rotation at 589 nm .

Discussion. Final atomic positional and thermal parameters are given in Table 1.*

The chief feature of the crystal structure is alternating layers of loosely packed molecules in the ac planes. Roughly planar molecules are approximately parallel with all others in a layer, and pack without close interaromatic contacts. In this motif, adjacent layers are inclined oppositely and related to one another by the screw axis along b. Fig. 1 shows a unit-cell view normal to these layers in the $b c$ plane. In detail, the molecules are of two configurational types, corresponding to a diastereomeric pair, in an ordered structure. This relatively rare result has also recently been observed in a cyclic tetrapetide (Chiang \& Karle, 1982). Along a, like molecules are hydrogen-bonded between hydroxyl and carbonyl groups. The $\mathrm{O} \cdots \mathrm{O}$ distances are 2.781 (7) (trans) and 2.780 (7) $\AA$ (cis). The cell volume is $1233 \AA^{3}$ compared with $1206 \AA^{3}$ for the racemate (Valente et al., 1979) and the melting point and density ( $404 \mathrm{~K}, 1.32 \mathrm{~g} \mathrm{~cm}^{-3}$ ) are lower than for the racemate ( $414 \mathrm{~K}, 1.35 \mathrm{~g} \mathrm{~cm}^{-3}$ ), which also contains two molecules in its asymmetric unit but has closer interaromatic contacts.

[^1]Fig. 1. A view of the unit cell projected nearly along a showing the layers in ac.

Two distinct molecular types are contained in the crystal and are grossly related by an approximate center of symmetry. The crystal structure therefore resembles a racemic structure in space group $P 2_{1} / n$, as if the molecules were centrosymmetrically related. The molecules differ, however, in both configuration and conformation. Both display an axial hydroxyl group corresponding to the more stable anomeric form and the configurations at their hemiketal carbons [ $C(13)$ ] are opposite. This is consistent with pseudo-inversion symmetry between the two molecules and is possible in an enantiomorphic compound such as this because the hemiketal inversion is labile in the solution from which the crystals form. The configuration at the other asymmetric center $[\mathrm{C}(11)$ ] determines the enantiomorphic form of the molecules. Brucine, the resolving agent, forms a salt with the coumarin 4-hydroxyl group of the molecule in the open side-chain form in which $C(11)$ is the only asymmetric center, and the hemiketals are formed later upon liberating the resolved compound. The configuration at $C(11)$ in the two molecules is the same and, referring to the spatial relationship of the 2-hydroxyl and 4-methyl groups, both cis and trans diastereomeric forms are present in the crystal. From a comparison of its circular dichroism spectrum with those from similar compounds of known absolute configuration, we can assign the cis isomer as $2 R, 4 R$ and the trans isomer as $2 S, 4 R$ (Valente \& Trager, 1978), where the 2 position is $C(13)$ and the 4 position is $\mathrm{C}(11)$ in Fig. 2. The cis isomer has the methyl [C(15)] disposed in a pseudoequatorial conformation. All other atoms in the structures are nearly inversionrelated except these methyls and hydrogen atoms bonded to $\mathrm{C}(11)$. A drawing of both molecules and this relationship is given in Fig. 2.


Fig. 2. A view of the two molecules in projection along $\mathbf{c}$, showing the near inversion symmetry and giving the atom-numbering scheme.

Table 2. Torsion angles $\left(^{\circ}\right.$ ) in the dihydropyran rings
E.s.d.'s are about $1 \cdot 0^{\circ}$.

cis
trans
$b$
-55
59

| $c$ | $d$ |
| ---: | ---: |
| 45 | -18 |
| -49 | 21 |



The conformations of the dihydropyran rings in the molecules are half-chairs distorted towards the $e f$ diplanar form. Intraring torsion angles are presented in Table 2. The flattening of the dihydropyran rings may also be seen in the deviation of $\mathrm{C}(12)$ and $\mathrm{C}(13)$ from the mean plane described by the four remaining ring atoms. In the cis molecule, they are -0.42 and $0.24 \AA$ from the mean plane; in the trans molecule, -0.54 and $0.19 \AA$. In general the average bond lengths and angles for the structure agree with those from similar structures (Valente et al., 1979). Average and maximal differences in bond lengths between the two different molecules are 0.030 and $0.052 \AA$, and in bond angles 2.2 and $7.7^{\circ}$. Considering the small data set, the parameter correlations, and anisotropy of many of the coumarin ring atoms, we consider the accuracy of individual structural dimensions to be no better than the average differences just quoted. This may still be an underestimation.

We thank Professor E. C. Lingafelter for valuable discussion and use of his facilities, Mr A. Aruffo for experimental assistance, and the Department of Chemistry for computational support. One of us (EJV) expresses thanks to Dr W. F. Trager, Department of Medicinal Chemistry, for his interest in the research and financial support.

## References

Chiang, C. C. \& Karle, I. L. (1982). Int. J. Pept. Protein Res. 20, 133-136.
Germain, G., Main, P. \& Woolfson, M. M. (1971). Acta Cryst. A27, 368-376.
Ikawa, M., Stahmann, M. \& Link, K. P. (1944). J. Am. Chem. Soc. 66, 902-906.
International Tables for $X$-ray Crystallography (1974). Vol. IV. Birmingham: Kynoch Press.
Stewart, R. F., Davidson, E. R. \& Simpson, W. T. (1965). J. Chem. Phys. 42, 3175-3187.
Valente, E., Santarsiero, B. \& Schomaker, V. (1979). J. Org. Chem. 44, 798-802.
Valente, E. \& Trager, W. F. (1978). J. Med. Chem. 21, 141-143.


[^0]:    * Current address: Department of Chemistry, Mississippi College, Clinton, MS 39058, USA.

[^1]:    * Lists of structure factors, anisotropic thermal parameters and H-atom positions have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39265 ( 16 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, Chester CHI 2HU, England.
    

